

2022

MATHEMATICS — GENERAL

Paper : GE/CC-4

Full Marks : 65

The figures in the margin indicate full marks.

*Candidates are required to give their answers in their own words
as far as practicable.*

Group - A

1. Choose the correct answer :

1×10

(a) Which of the following set is a group with respect to addition

(i) $\{-3, -2, -1, 0, 1, 2, 3\}$

(ii) $\{-1, 1\}$

(iii) $\{-1, 0, 1\}$

(iv) $\{0\}$.

(b) -2 is an eigenvalue of the matrix $M = \begin{pmatrix} 2 & -2 & 3 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{pmatrix}$. Then M^{-1} has an eigenvalue

(i) -2

(ii) 1

(iii) 2

(iv) $-\frac{1}{2}$

(c) Probability that at least one of the events A and B occurs is

(i) $P(A) + P(B) - P(AB)$

(ii) $P(A) + P(B) + 2P(AB)$

(iii) $P(A) + P(B) + P(AB)$

(iv) $P(A) + P(B) - 2P(AB)$

(d) Number of divisor of zero in the Ring $(\mathbb{Z}_5, \oplus, \odot)$ is

(i) 0

(ii) 1

(iii) 2

(iv) 3

(e) If $(0, 1, 3) = a(2, 1, 1) + b(4, 2, 2)$, then the values of a and b are

(i) $(1, 1)$

(ii) $(-1, 1)$

(iii) $(0, 0)$

(iv) None of these.

Please Turn Over

- (f) For the probability density function given by $f(x) = \begin{cases} e^{-x}, & x \geq 0 \\ 0, & \text{elsewhere} \end{cases}$

the mean is

- (i) 1 (ii) $\frac{1}{2}$
 (iii) 2 (iv) 4
- (g) If $E(T_1) = \theta_1 + \theta_2$ and $E(T_2) = \theta_1 - \theta_2$, then the unbiased estimator of θ_1 is
- (i) $T_1 + T_2$ (ii) $\frac{1}{2}(T_1 - T_2)$
 (iii) $\frac{1}{2}(T_1 + T_2)$ (iv) $\frac{1}{2}(T_2 - T_1)$
- (h) Binary number corresponding to the decimal number 27.625 is
- (i) 11011.101 (ii) 10111.101
 (iii) 11101.011 (iv) 11011.011
- (i) Which of the following can be a variable name in C?
- (i) Volatile (ii) True
 (iii) Friend (iv) Export.
- (j) The value of the FORTRAN expression : $(A*(B + C))/D + A$, where $A = 3$, $B = 5$, $C = -2$ and $D = 4$ is
- (i) 3 (ii) 4
 (iii) 5 (iv) 6

Group-B

Unit-1

(Algebra - II)

2. Answer *any three* questions :

5×3

- (a) Prove that the set $Q \setminus \{-1\}$ is a group with respect to the composition 'o' defined by $aob = a + b + ab$. Is it abelian?
- (b) Show that the ring of matrix $\left[\begin{pmatrix} a & b \\ 2b & a \end{pmatrix} : a, b \in \mathbb{R} \right]$ does not form a Field, \mathbb{R} being the set of all real numbers.
- (c) Is the set $U = \{(x, y, z) \in \mathbb{R}^3 : x - 2y + 3z = 0\}$ a subspace of the real vector space \mathbb{R}^3 ? If so, find the basis and dimension of this subspace.

(3)

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(d) Find the eigenvalues and eigenvectors of the matrix $\begin{pmatrix} 1 & -1 & 2 \\ 2 & -2 & 4 \\ 3 & -3 & 6 \end{pmatrix}$.

(e) Show that the real quadratic form $5x^2 + y^2 + 14z^2 - 4yz - 10zx$ is positive definite.

Unit-2

(Computer Science and Programming)

3. Answer *any four* questions :

(a) Find the product of $(11,0011)_2$ and $(10,01)_2$ and also find the octal and hexadecimal equivalents of the product. 5

(b) Draw a flowchart for computing the g.c.d. of two positive integers m and n . 5

(c) (i) Let $A = 2.7$, $B = 3.5$ and $L = \text{ABS}(A - 3.*B)/5$. Find what will be stored at L .

(ii) Write FORTRAN expression of $\frac{\sqrt{a + \log_e b}}{c + d \sin x}$ 2+3

(d) Write an algorithm to sort n given integers in descending order. 5

(e) Write a FORTRAN program to find the area of a triangle whose three sides are given. 5

(f) What is positional number system? Why are binary numbers used in computer design? 2+3

(g) Write a FORTRAN program to check whether a year is a Leap year or not. 5

Unit-3

(Probability and Statistics)

4. Answer *any four* questions : 5×4

(a) Bag A contains 2 white and 3 red balls; and bag B contains 4 white and 5 red balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from bag B .

(b) Four persons are chosen at random from a group containing 3 men, 2 women and 4 children. Show that the chances that exactly two of them will be children is $\frac{10}{21}$.

(c) Find the coefficient of correlation from the following data :

x	0	1	2	3	4
f	2	3	5	10	5

(d) Draw a Histogram from the following distribution :

Age Group	14-15	16-17	18-20	21-24	25-29	30-34	35-39
No. of wage earners	60	140	150	110	110	100	90

Please Turn Over

- (e) The population of scores of 10 years children in a test is known to have a standard deviation 5.2. If a random sample of size 20 shows a mean of 16.9, find 95% confidence interval for the mean score of the population, assuming that the population is normal.

$$\left(\text{Given that } \frac{1}{\sqrt{2\pi}} \int_{1.96}^{\infty} e^{-\frac{x^2}{2}} dx = 0.025 \right).$$

- (f) If the equations of two regression lines obtained in a correlation analysis are $2y + x = 11$ and $2x + 3y - 18 = 0$, determine which one of them is the regression equation of x on y . Find the means and correlation coefficient of x and y .
- (g) In a random sample of size 400 there are 80 defective items. Test at 5% level whether the proportion of defective items in the population may be regarded as $\frac{1}{6}$.

$$\left[\text{Given } \int_0^{1.96} \phi(t) dt = 0.475, \phi \text{ is the pdf of normal variate} \right].$$
